

## CO<sub>2</sub> Reduction Reaction to Create CH<sub>4</sub> and CH<sub>3</sub>OH on Chromium Doped Silicon, Carbon and Boron Nitride (2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub>)

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(Received on 30<sup>th</sup> April 2025, accepted in revised form 24<sup>th</sup> December 2025)

**Abstract:** Here, the pathways for CO<sub>2</sub> reduction reaction to create CH<sub>4</sub> and CH<sub>3</sub>OH on Si<sub>76</sub>, C<sub>76</sub> and B<sub>38</sub>N<sub>38</sub> as catalysts are investigated. The effects of adsorption of Cr on capacities of Si<sub>76</sub>, C<sub>76</sub> and B<sub>38</sub>N<sub>38</sub> for CO<sub>2</sub>-RR are examined. Results shown that the over-potential of CO<sub>2</sub>-RR on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> are lower than Fe, Ni and Co single atom as catalysts, Cu, Au, Ag based bimetallic catalysts and Pt and Pd as metal catalysts in previous works. The  $\Delta G_{\text{reaction}}$  of possible reaction steps of CO<sub>2</sub> reduction on 2Cr-Si<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages are more negative than 2Cr-C<sub>76</sub> nanocage. The over-potential for production of CH<sub>4</sub> and CH<sub>3</sub>OH are lower than creation of HCOOH and HCHO on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages. The over-potential for CO, HCOOH, HCHO, CH<sub>3</sub>OH and CH<sub>4</sub> production on 2Cr-B<sub>38</sub>N<sub>38</sub> nanocage is 0.34, 0.27, 0.31, 0.24 and 0.22 V. The 2Cr-Si<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> are catalyzed the reaction steps of CO<sub>2</sub>-RR by three pathways and high performance.

**Keyword:** Nano-catalysts, CH<sub>3</sub>OH, CO<sub>2</sub>-RR, CH<sub>4</sub>, reduction reaction mechanism, Metal adsorption.

### Introduction

The carbon dioxide (CO<sub>2</sub>) has been produced from fossil fuels [1] and CO<sub>2</sub> are one of the main reasons for earth warming [2]. The decreasing and removing the CO<sub>2</sub> has high important to reduce the earth warming [3-5]. The CO<sub>2</sub> can be removed in important reactions and CO<sub>2</sub> can be converted to other species with high performances [5-8]. The organic chemists have confirmed that the reduction reaction of CO<sub>2</sub> can create the HCOOH and CH<sub>3</sub>OH molecules [9-11].

The Si and C nanocages and nanotubes have been proposed the novel pathways to design of stable and active catalysts for important reaction in chemical industry [12-14]. The capacities of metals doped Si and C nanocages and nanotubes to catalyze the important organic reactions in chemical industry have been examined [15-17]. Researchers shown than the Si, BN and C nanocages and nanotubes have effective properties for CO<sub>2</sub>-RR in normal temperature [17]. In recent years, researchers have shown that the metal catalysts due to their high price, low stability, low selectivity and low performances have low efficiency for oxidation and reduction of toxic gases [11-15].

In previous works [11-15] the capacities of various metal catalysts including the Fe, Ni and Co single atom, Cu, Au, Ag based bimetallic and Pt and Pd as

catalysts for CO<sub>2</sub>-RR have been examined. The possible pathways for CO<sub>2</sub>-RR on various metal catalysts including the Fe, Ni and Co single atom, Cu, Au, Ag based bimetallic and Pt and Pd have been investigated [11-15]. Results have shown that the metal catalysts (Fe, Ni and Co single atom, Cu, Au, Ag based bimetallic and Pt and Pd) have high price and low selectivity for catalyze the reaction steps of CO<sub>2</sub>-RR in normal temperature [11-15].

In this work, the pathways for CO<sub>2</sub>-RR for formation the CO, CH<sub>4</sub>, HCOOH, HCHO and CH<sub>3</sub>OH species on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> are investigated. The effects of adsorption of Cr atoms of 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> on their capacities for CO<sub>2</sub>-RR are examined. The capacities of 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> for CO<sub>2</sub>-RR are compared. The catalysts and pathways on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> for CO<sub>2</sub>-RR are proposed with high efficiency. The goals of this work are: to compare the abilities of 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> of CO<sub>2</sub>-RR; to suggest the new catalysts (2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub>) for CO<sub>2</sub>-RR, to compare the catalytic activity of various nanocages for CO<sub>2</sub>-RR, to find the effective pathways for CO<sub>2</sub>-RR, to compare the efficiency of 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> for CO<sub>2</sub>-RR with metal based catalysts.

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### Computational Details

The M06-2X/6-311+G (2d, 2p), PBEPBE/6-311+G (2d, 2p) and B3LYP-D3/6-311+G (2d, 2p) methods have been used to optimize the Si<sub>76</sub>, C<sub>76</sub>, B<sub>38</sub>N<sub>38</sub>, 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages and their complexes with species in GAMESS software [16]. In this study the transition states of reaction step of CO<sub>2</sub>-RR on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> have been obtained with opt=qst3 and results have shown that there is only one imaginary frequency for transition states of reaction step of CO<sub>2</sub>-RR on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> [17-19]. In this study the COSMO (Conductor-like screening model) model as an implicit solvation model has been used to consider the effects of solvent (water as polar solvent) on reaction steps of possible mechanisms of CO<sub>2</sub>-RR by M06-2X /6-311+G (2d, 2p) method [20].

In this study, the acceptable spin states and spin multiplicities (S = 3, 2 and 1 and 2S+1 = 7, 5 and 3) of Cr atoms in 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> and complexes of 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> with intermediates of CO<sub>2</sub>-RR have been considered [19, 20]. The complexes of intermediates of CO<sub>2</sub>-RR have been optimized and their frequencies have been calculated [20]. The adsorption free Gibbs energies ( $\Delta G_{\text{adsorption}}$ ) of CO<sub>2</sub> and intermediates of CO<sub>2</sub>-RR on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> are calculated [21]:

$$\Delta G_{\text{adsorption}} = G_{\text{specie-nanocage}} - G_{\text{specie}} - G_{\text{nanocage}} \quad (1)$$

The  $G_{\text{nanocage}}$  is free Gibbs energies of 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages and  $G_{\text{specie}}$  is free Gibbs energies of intermediates of CO<sub>2</sub> reduction reactions and the  $G_{\text{specie-nanocage}}$  is free Gibbs energies of complexes of 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages with intermediates of CO<sub>2</sub> reduction reactions [19].

The  $\Delta G_{\text{reaction}}$  of reaction steps of CO<sub>2</sub> reduction reactions on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> are calculated [20-23]:

$$\Delta G_{\text{reaction}} = \Delta E + \Delta ZPE - T\Delta S + eU + \Delta G_{\text{pH}} \quad (2)$$

The T, E, S and ZPE are temperature, energy, entropy and zero-point energy of complexes of Si<sub>76</sub>, C<sub>76</sub>, B<sub>38</sub>N<sub>38</sub>, 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> with species [24]. The  $\Delta G_{\text{pH}}$  as free energy correction because of variations in H<sup>+</sup> concentration can be calculated by  $G_{\text{pH}} = -kT \ln [H^+] = kT \ln 10 \times \text{pH}$ , and pH is 0. The U and e are applied potential and number of electron transfer, respectively [24]. The U is potential of electrode commissioned to electrode of standard hydrogen and the values of U is started since 0 until 1.23 V in balance potential U<sub>0</sub> and several stages of CO<sub>2</sub>-RR are formidable. The used potential U is requested to eliminate positive part of Gibbs free energy and

overvoltage is defined as  $\eta = U_0 - U$  [24, 25]. The zero-point energy and entropy contributions of nanocages (Si<sub>76</sub>, C<sub>76</sub> and B<sub>38</sub>N<sub>38</sub>), metal doped nanocages (2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub>) and their complexes of intermediates of reaction steps of CO<sub>2</sub>-RR on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> have been calculated by vibrational frequencies of optimized structures by M06-2X /6-311+G (2d, 2p) method [17-20].

### Results and Discussion

*Nanocages (Si<sub>76</sub>, C<sub>76</sub> and B<sub>38</sub>N<sub>38</sub> and 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub>)*

The properties of Si<sub>76</sub>, C<sub>76</sub> and B<sub>38</sub>N<sub>38</sub> nanocages and 2Cr-doped structures (2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub>) are investigated. The Si<sub>76</sub>, C<sub>76</sub>, B<sub>38</sub>N<sub>38</sub>, 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages are presented in Figure 1. The  $\Delta G_{\text{adsorption}}$  [25-28] values of Cr on Si<sub>76</sub>, C<sub>76</sub> and B<sub>38</sub>N<sub>38</sub> are examined in Table 1:

$$\Delta G_{\text{adsorption}} = G_{2\text{Cr-nanocage}} - G_{\text{nanocage}} - 2G_{\text{Cr}} \quad (3)$$

The  $G_{\text{nanocage}}$  is free Gibbs energies of Si<sub>76</sub>, C<sub>76</sub> and B<sub>38</sub>N<sub>38</sub> nanocages and  $G_{\text{Cr}}$  is free Gibbs energy of Cr and  $G_{2\text{Cr-nanocage}}$  is free Gibbs energies of Cr with Si<sub>76</sub>, C<sub>76</sub> and B<sub>38</sub>N<sub>38</sub>. The  $\Delta G_{\text{adsorption}}$  of 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages are -6.79, -6.21 and -6.46 eV. The 2Cr-Si<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages have higher  $\Delta G_{\text{adsorption}}$  than 2Cr-C<sub>76</sub> nanocage. The  $\Delta G_{\text{adsorption}}$  of 2Cr-C<sub>76</sub> nanocage are lower than 2Cr-Si<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages ca 0.51 and 0.25 eV. The values of  $\Delta G_{\text{adsorption}}$  for Cr on Si<sub>76</sub>, C<sub>76</sub> and B<sub>38</sub>N<sub>38</sub> are all negative pointing out that this process is exothermic.

The formation energies ( $\Delta E_{\text{formation}}$ ) of Si<sub>76</sub>, C<sub>76</sub> and B<sub>38</sub>N<sub>38</sub> nanocages and 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> are examined [29] in Table 1:

$$\Delta E_{\text{formation}} = E_{\text{nanocage}} - 76 * E_{\text{X}} \quad (4)$$

$$\Delta E_{\text{formation}} = E_{2\text{Cr-nanocage}} - E_{\text{nanocage}} - 2 * E_{\text{Cr}} \quad (5)$$

The  $E_{2\text{Cr-nanocage}}$  is energies of Cr with 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub>, the  $E_{\text{nanocage}}$  is energies of nanocages, the  $E_{\text{Cr}}$  is energy of Cr atom and  $E_{\text{X}}$  is energies of Si, C and BN. The  $\Delta E_{\text{formation}}$  of 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages are -5.25, -4.95 and -5.19 eV. The 2Cr-Si<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages have higher  $\Delta E_{\text{formation}}$  than 2Cr-C<sub>76</sub> nanocage. In this study, the relative energy for acceptable spin states and spin multiplicities (S = 3, 2 and 1 and 2S+1 = 7, 5 and 3) of Cr atoms in 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> are reported in Table 2. The  $\Delta E_{\text{formation}}$  of 2Cr-C<sub>76</sub> nanocage is lower than 2Cr-Si<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages ca 0.31 and 0.23 eV. The values of  $\Delta E_{\text{formation}}$  of Si<sub>76</sub>, C<sub>76</sub>, B<sub>38</sub>N<sub>38</sub>, 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> are all negative. The  $\Delta E_{\text{formation}}$  of Si and BN nanocages are higher than C nanocages.

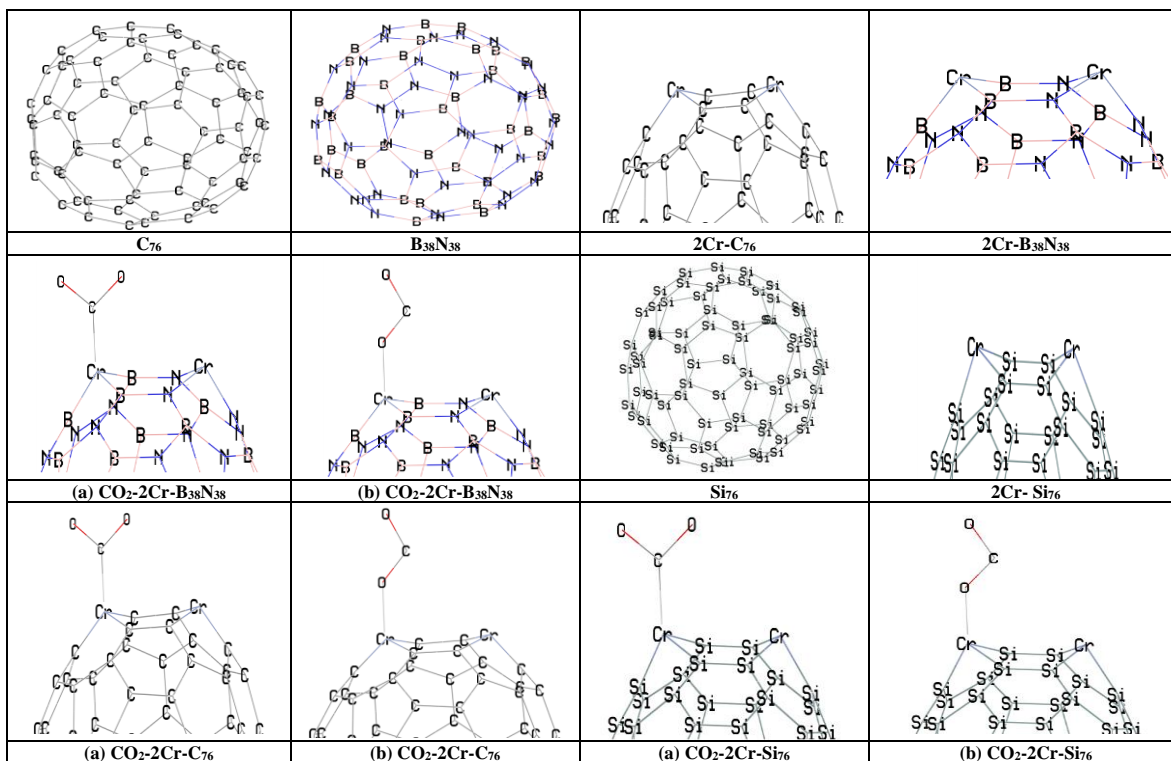


Fig. 1: Structures of  $Si_{76}$ ,  $C_{76}$  and  $B_{38}N_{38}$  nanocages,  $2Cr-Si_{76}$ ,  $2Cr-C_{76}$  and  $2Cr-B_{38}N_{38}$  nanocages and complexes with  $CO_2$ .

Table-1: The  $\Delta E_{formation}$  and  $\Delta G_{adsorption}$  of  $2Cr-Si_{76}$ ,  $2Cr-C_{76}$  and  $2Cr-B_{38}N_{38}$  nanocages, the  $\Delta G_{adsorption}$  of  $CO_2$  reduction reactions on  $2Cr-Si_{76}$ ,  $2Cr-C_{76}$  and  $2Cr-B_{38}N_{38}$  nanocages.

M06-2X/6-311+G (2d, 2p)			
Nanocages	$2Cr-C_{76}$	$2Cr-B_{38}N_{38}$	$2Cr-Si_{76}$
$\Delta E_{formation}$	-4.95	-4.95	-5.19
$\Delta G_{adsorption}$	-6.21	-6.21	-6.46
$\Delta G_{adsorption}$	$2Cr-C_{76}$	$2Cr-B_{38}N_{38}$	$2Cr-Si_{76}$
$CO_2$ (a)	-0.99	-1.07	-1.20
$CO_2$ (b)	-0.90	-0.97	-1.09
CO	-2.81	-3.03	-3.41
HCOOH	-1.60	-1.73	-1.95
HCHO	-2.00	-2.16	-2.43
$CH_3OH$	-1.73	-1.86	-2.09
$CH_4$	-0.85	-0.92	-1.04
PBPBE/6-311+G (2d, 2p)			
Nanocages	$2Cr-C_{76}$	$2Cr-B_{38}N_{38}$	$2Cr-Si_{76}$
$\Delta E_{formation}$	-4.89	-4.86	-5.10
$\Delta G_{adsorption}$	-6.10	-6.10	-6.34
$\Delta G_{adsorption}$	$2Cr-C_{76}$	$2Cr-B_{38}N_{38}$	$2Cr-Si_{76}$
$CO_2$ (a)	-0.97	-1.05	-1.18
$CO_2$ (b)	-0.88	-0.95	-1.07
CO	-2.76	-2.98	-3.35
HCOOH	-1.57	-1.70	-1.91
HCHO	-1.96	-2.12	-2.39
$CH_3OH$	-1.70	-1.83	-2.05
$CH_4$	-0.83	-0.90	-1.02
B3LYP-D3/6-311+G (2d, 2p)			
Nanocages	$2Cr-C_{76}$	$2Cr-B_{38}N_{38}$	$2Cr-Si_{76}$
$\Delta E_{formation}$	-4.92	-4.92	-5.15
$\Delta G_{adsorption}$	-6.17	-6.17	-6.41
$\Delta G_{adsorption}$	$2Cr-C_{76}$	$2Cr-B_{38}N_{38}$	$2Cr-Si_{76}$
$CO_2$ (a)	-0.98	-1.06	-1.18
$CO_2$ (b)	-0.89	-0.96	-1.07
CO	-2.77	-2.99	-3.36
HCOOH	-1.58	-1.71	-1.92
HCHO	-1.97	-2.13	-2.40
$CH_3OH$	-1.71	-1.83	-2.06
$CH_4$	-0.84	-0.91	-1.03

*CO<sub>2</sub>-RR to CO, CH<sub>4</sub>, HCOOH, HCHO and CH<sub>3</sub>OH on surfaces of 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages*

In this section the potential of 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages to catalyze the CO<sub>2</sub>-RR to CH<sub>4</sub> and CH<sub>3</sub>OH is investigated. The three mechanisms for CO<sub>2</sub>-RR (Pathway 1: \*CO<sub>2</sub> → \*COOH → \*CO → \*CHO → \*CH<sub>2</sub>O → \*CH<sub>3</sub>O → CH<sub>3</sub>OH → \*O + CH<sub>4</sub>; Pathway 2: \*CO<sub>2</sub> → \*OCHO → \*-HCOOH → \*CHO → \*HCHO and Pathway 3: \*CO<sub>2</sub> → \*COOH → \*-HCOOH) are investigated. The adsorption of CO<sub>2</sub> on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> is investigated. The structures of complexes of CO<sub>2</sub> on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages are presented in Figure 1. The calculated ΔG<sub>adsorption</sub> of CO<sub>2</sub> on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> are summarized in Table 1.

The ΔG<sub>adsorption</sub> of CO<sub>2</sub> on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages via position *a* are -1.20, -0.99 and -1.07 eV. The ΔG<sub>adsorption</sub> of CO<sub>2</sub> on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages via position *b* are -1.09, -0.90 and -0.97 eV. The Cr atoms of 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages is adsorbed the CO<sub>2</sub> by O and C. The ΔG<sub>adsorption</sub> of CO<sub>2</sub> on 2Cr-C<sub>76</sub> nanocage via positions *a* and *b* are lower than 2Cr-Si<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages ca 0.19 and 0.08 eV. The ΔG<sub>adsorption</sub> of CO<sub>2</sub> on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages via position *a* are higher than position *b* ca 0.09 to 0.11 eV. The 2Cr-Si<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages have higher ΔG<sub>adsorption</sub> than 2Cr-C<sub>76</sub> nanocage [30-32]. The structures of CO<sub>2</sub>-RR to create the CO, CH<sub>4</sub>, HCOOH, HCHO and CH<sub>3</sub>OH on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> are presented in Figure 2. In this study, the relative energy for acceptable spin states and spin multiplicities (*S* = 3, 2 and 1 and 2*S*+1

= 7, 5 and 3) of Cr atoms in complexes of 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> with intermediates of reaction steps of CO<sub>2</sub>-RR are reported in Table-2.

The ΔG<sub>reaction</sub> and E<sub>barrier</sub> of reaction steps of CO<sub>2</sub>-RR on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages are presented in Table 3. After adsorption of CO<sub>2</sub> on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages is CO<sub>2</sub> protonation to create the nanocage-\*COOH and nanocage-\*OCHO [33, 34]. The ΔG<sub>reaction</sub> of formation of nanocage-\*OCHO on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages are -0.44, -0.36 and -0.39 eV. The E<sub>barrier</sub> of formation of nanocage-\*OCHO on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages are 0.23, 0.26 and 0.24 eV. The ΔG<sub>reaction</sub> of formation of nanocage-\*COOH on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages are -0.35, -0.28 and -0.31 eV. The E<sub>barrier</sub> of formation of nanocage-\*COOH on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages are 0.15, 0.17 and 0.16 eV.

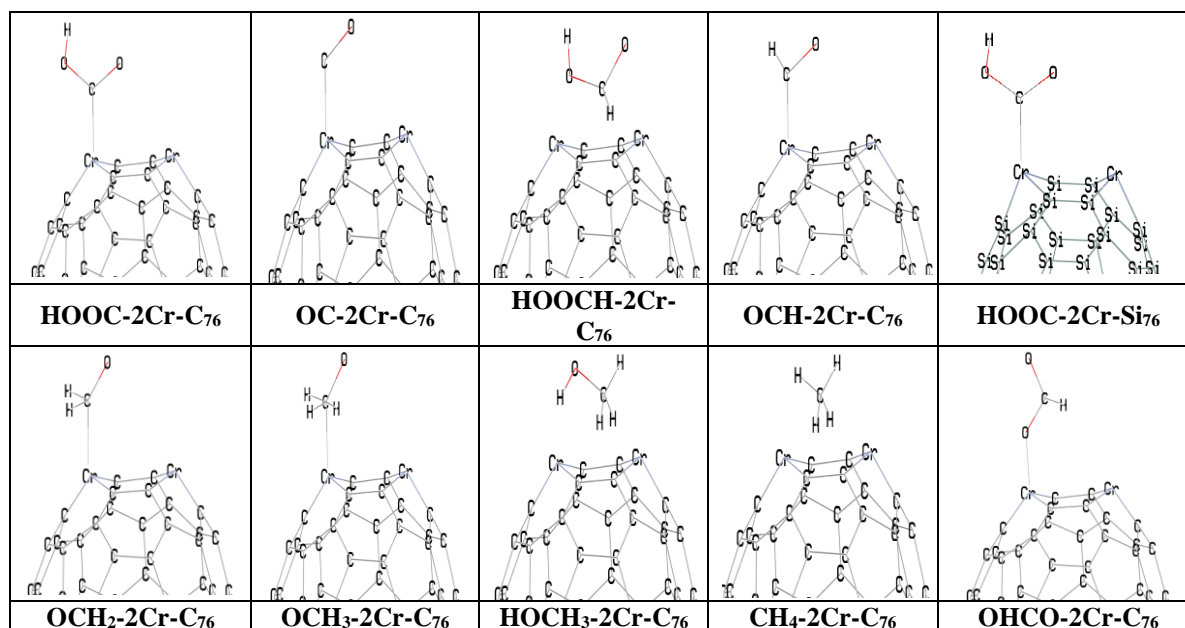
The E<sub>barrier</sub> of nanocage-\*OCHO is higher than nanocage-\*COOH on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages. The ΔG<sub>reaction</sub> of \*OCHO is more negative than \*COOH on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages and the \*COOH and \*OCHO are created to other possible species. The \*CO is produced from \*COOH on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub>. The CO desorption is required high ΔG<sub>reaction</sub> and CO production has low efficiency on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub>. The ΔG<sub>reaction</sub> of formation of nanocage-\*CO on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages are -0.37, -0.30 and -0.32 eV. The E<sub>barrier</sub> of formation of nanocage-\*CO on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages are 0.23, 0.26 and 0.24 eV. The \*COOH and \*OCHO on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> are converted to HCOOH.

Table-2: The relative energy in eV of 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages (*S* = 3, 2 and 1 and 2*S*+1 = 7, 5 and 3) and their complexes with intermediates of CO<sub>2</sub> reduction reactions.

Relative energy	2Cr-C <sub>76</sub>			2Cr-B <sub>38</sub> N <sub>38</sub>			2Cr-Si <sub>76</sub>		
<i>S</i>	1	2	3	1	2	3	1	2	3
2 <i>S</i> + 1	3	5	7	3	5	7	3	5	7
Relative energy	0.0452	0.0283	0.000	0.0416	0.0237	0.000	0.0473	0.0266	0.000
Complexes	2Cr-C <sub>76</sub>			2Cr-B <sub>38</sub> N <sub>38</sub>			2Cr-Si <sub>76</sub>		
<i>S</i>	1	2	3	1	2	3	1	2	3
2 <i>S</i> + 1	3	5	7	3	5	7	3	5	7
CO <sub>2</sub> (a)	0.0450	0.0280	0.0000	0.0410	0.0230	0.0000	0.0470	0.0260	0.0000
CO <sub>2</sub> (b)	0.0444	0.0276	0.0000	0.0405	0.0227	0.0000	0.0464	0.0257	0.0000
CO	0.0415	0.0258	0.0000	0.0378	0.0212	0.0000	0.0433	0.0240	0.0000
HCOOH	0.0403	0.0251	0.0000	0.0367	0.0206	0.0000	0.0421	0.0233	0.0000
HCHO	0.0389	0.0242	0.0000	0.0354	0.0199	0.0000	0.0406	0.0225	0.0000
CHO	0.0374	0.0233	0.0000	0.0341	0.0191	0.0000	0.0391	0.0216	0.0000
CH <sub>2</sub> O	0.0356	0.0221	0.0000	0.0324	0.0182	0.0000	0.0371	0.0205	0.0000
CH <sub>3</sub> O	0.0351	0.0218	0.0000	0.0320	0.0179	0.0000	0.0367	0.0203	0.0000
CH <sub>3</sub> OH	0.0331	0.0206	0.0000	0.0302	0.0169	0.0000	0.0346	0.0191	0.0000
CH <sub>4</sub>	0.0305	0.0190	0.0000	0.0278	0.0156	0.0000	0.0318	0.0176	0.0000

Table-3: The  $E_{activation}$ ,  $\Delta G_{reaction}$  in eV of  $CO_2$ -RR on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages.

Nanocages	M06-2X/6-311+G (2d, 2p)					
	2Cr-C <sub>76</sub>		2Cr-B <sub>38</sub> N <sub>38</sub>		2Cr-Si <sub>76</sub>	
$CO_2$ reduction reaction	Eactivation	$\Delta G_{reaction}$	Eactivation	$\Delta G_{reaction}$	Eactivation	$\Delta G_{reaction}$
*CO <sub>2</sub> → *COOH	0.17	-0.28	0.16	-0.31	0.15	-0.35
*COOH → *CO	0.26	-0.30	0.24	-0.32	0.23	-0.37
*CO → *CHO	0.14	0.27	0.13	0.29	0.12	0.33
*CHO → *CH <sub>2</sub> O	0.27	0.24	0.25	0.26	0.24	0.30
*CH <sub>2</sub> O → *CH <sub>3</sub> O	0.13	-0.43	0.12	-0.47	0.11	-0.53
*CH <sub>3</sub> O → CH <sub>3</sub> OH	0.40	-0.66	0.37	-0.71	0.35	-0.81
*CH <sub>3</sub> O → *O + CH <sub>4</sub>	0.28	-1.38	0.26	-1.48	0.25	-1.70
*COOH → *-HCOOH	0.47	0.19	0.43	0.21	0.41	0.23
*CO <sub>2</sub> → *OCHO	0.26	-0.36	0.24	-0.39	0.23	-0.44
*OCHO → *-HCOOH	0.38	-0.08	0.35	-0.09	0.33	-0.10
*HCOOH → *CHO	0.51	-0.13	0.48	-0.13	0.46	-0.16
*CHO → *HCHO	0.36	-0.64	0.34	-0.69	0.32	-0.79
<b>PBPBE/6-311+G (2d, 2p)</b>						
*CO <sub>2</sub> → *COOH	0.16	-0.29	0.15	-0.32	0.14	-0.36
*COOH → *CO	0.25	-0.31	0.23	-0.33	0.22	-0.38
*CO → *CHO	0.13	0.28	0.12	0.30	0.11	0.34
*CHO → *CH <sub>2</sub> O	0.26	0.25	0.24	0.27	0.23	0.31
*CH <sub>2</sub> O → *CH <sub>3</sub> O	0.12	-0.44	0.11	-0.49	0.10	-0.55
*CH <sub>3</sub> O → CH <sub>3</sub> OH	0.38	-0.68	0.35	-0.73	0.33	-0.84
*CH <sub>3</sub> O → *O + CH <sub>4</sub>	0.26	-1.43	0.25	-1.53	0.24	-1.76
*COOH → *-HCOOH	0.44	0.20	0.41	0.22	0.39	0.24
*CO <sub>2</sub> → *OCHO	0.25	-0.37	0.23	-0.40	0.22	-0.46
*OCHO → *-HCOOH	0.36	-0.08	0.33	-0.09	0.31	-0.10
*HCOOH → *CHO	0.48	-0.13	0.45	-0.13	0.43	-0.17
*CHO → *HCHO	0.34	-0.66	0.32	-0.71	0.30	-0.82
<b>B3LYP-D3/6-311+G (2d, 2p)</b>						
*CO <sub>2</sub> → *COOH	0.16	-0.29	0.15	-0.32	0.14	-0.37
*COOH → *CO	0.24	-0.31	0.22	-0.33	0.22	-0.39
*CO → *CHO	0.13	0.28	0.12	0.30	0.11	0.34
*CHO → *CH <sub>2</sub> O	0.25	0.25	0.23	0.27	0.22	0.31
*CH <sub>2</sub> O → *CH <sub>3</sub> O	0.12	-0.45	0.11	-0.49	0.10	-0.55
*CH <sub>3</sub> O → CH <sub>3</sub> OH	0.37	-0.69	0.35	-0.74	0.33	-0.85
*CH <sub>3</sub> O → *O + CH <sub>4</sub>	0.26	-1.44	0.24	-1.55	0.23	-1.78
*COOH → *-HCOOH	0.44	0.20	0.40	0.22	0.38	0.24
*CO <sub>2</sub> → *OCHO	0.24	-0.38	0.22	-0.41	0.22	-0.46
*OCHO → *-HCOOH	0.36	-0.08	0.33	-0.09	0.31	-0.10
*HCOOH → *CHO	0.48	-0.14	0.45	-0.14	0.43	-0.17
*CHO → *HCHO	0.34	-0.67	0.32	-0.72	0.30	-0.83



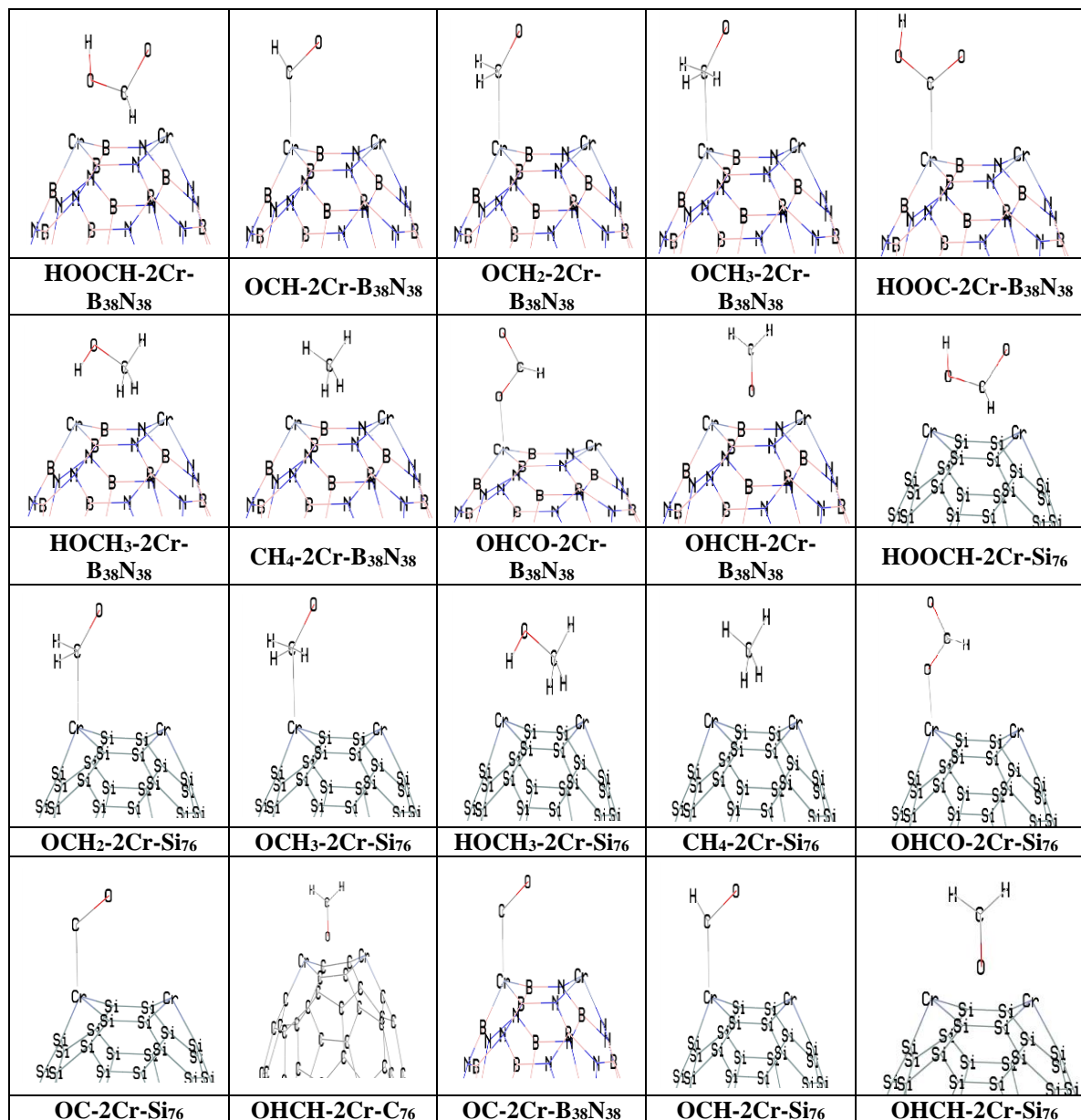


Fig. 2: Structures of complexes of CO<sub>2</sub>-RR derivatives with 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages.

The  $\Delta G_{\text{reaction}}$  values of reaction steps of CO<sub>2</sub>-RR (Pathway 1: \*CO<sub>2</sub> → \*COOH → \*CO → \*CHO → \*CH<sub>2</sub>O → \*CH<sub>3</sub>O → CH<sub>3</sub>OH → \*O + CH<sub>4</sub>; Pathway 2: \*CO<sub>2</sub> → \*OCHO → \*-HCOOH → \*CHO → \*HCHO and Pathway 3: \*CO<sub>2</sub> → \*COOH → \*-HCOOH) on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages are presented in Figures 3, and the Gibbs free energy plan of reaction steps of CO<sub>2</sub>-RR on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages in various U values are presented in Figures 4. The \*CO<sub>2</sub> → \*OCHO → HCOOH reactions is favored pathway and

$\Delta G_{\text{reaction}}$  of formation of nanocage-\*OCHO on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages are -0.44, -0.36 and -0.39 eV. The E<sub>barrier</sub> of formation of nanocage-\*OCHO on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages are 0.23, 0.26 and 0.24 eV. The CO and HCOOH creation on 2Cr-B<sub>38</sub>N<sub>38</sub> have higher  $\Delta G_{\text{reaction}}$  and lower E<sub>barrier</sub> than 2Cr-Si<sub>76</sub> and 2Cr-C<sub>76</sub>. The \*COOH → \*CO + H<sub>2</sub>O is rate-limiting on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages.

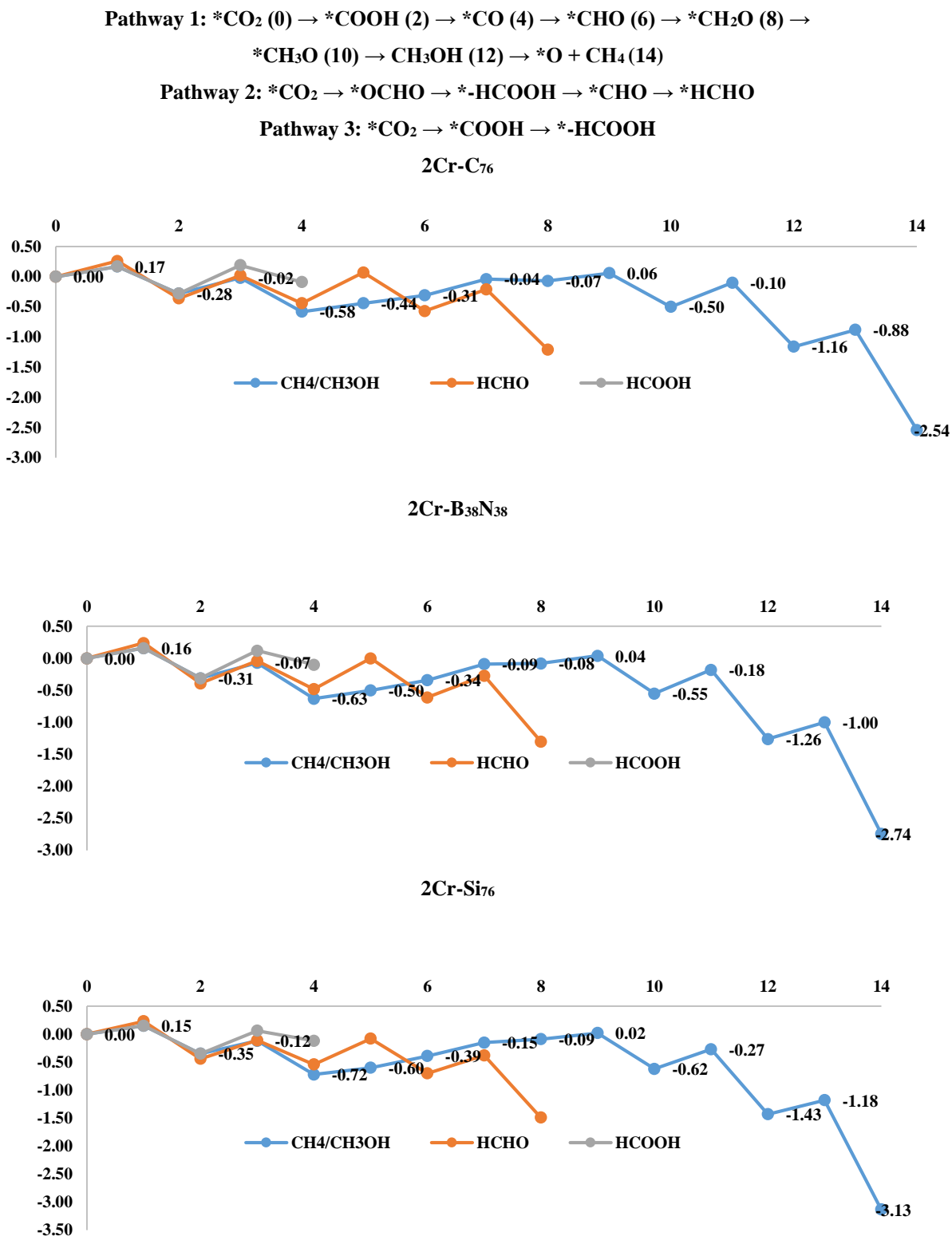


Fig. 3: The  $\Delta G_{\text{reaction}}$  of reaction steps of  $\text{CO}_2$ -RR on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages.

The CH<sub>3</sub>OH creation on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> is done by acceptable pathways and \*CO → \*CHO is rate limiting on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub>. The values of ΔG<sub>reaction</sub> of CH<sub>3</sub>OH creation on 2Cr-Si<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages are more negative than 2Cr-C<sub>76</sub> nanocage. The ΔG<sub>reaction</sub> of formation of nanocage-\*CH<sub>3</sub>O on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages are -0.53, -0.43 and -0.47 eV. The E<sub>barrier</sub> of formation of nanocage-\*CH<sub>3</sub>O on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages are 0.11, 0.13 and 0.12 eV. The reaction of CH<sub>3</sub>OH creation on 2Cr-Si<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages have lower E<sub>barrier</sub> than 2Cr-C<sub>76</sub> nanocage, significantly.

The HCHO creation on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages is processed. The \*CO → \*CHO is rate-limiting of HCHO production on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages. The ΔG<sub>reaction</sub> of formation of nanocage-\*CHO on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages are 0.33, 0.27 and 0.29 eV. The E<sub>barrier</sub> of formation of nanocage-\*CHO on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages are 0.12, 0.14 and 0.13 eV. The CO<sub>2</sub> is hydrogenated on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> and CH<sub>4</sub> is created and rate limiting is the \*CO → \*CHO.

Results shown that the \*CH<sub>3</sub>O → CH<sub>3</sub>OH reaction step for CO<sub>2</sub>-RR via pathway 1 (\*CO<sub>2</sub> → \*COOH → \*CO → \*CHO → \*CH<sub>2</sub>O → \*CH<sub>3</sub>O → CH<sub>3</sub>OH → \*O + CH<sub>4</sub>) on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> is the rate-limiting step for CO<sub>2</sub>-RR via pathway 1. The \*HCOOH → \*CHO reaction step for CO<sub>2</sub>-RR via pathway 2 (\*CO<sub>2</sub> → \*OCHO → \*-HCOOH → \*CHO → \*HCHO) on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> is the

rate-limiting step for CO<sub>2</sub>-RR via pathway 2. The \*COOH → \*-HCOOH reaction step for CO<sub>2</sub>-RR via pathway 3 (\*CO<sub>2</sub> → \*COOH → \*-HCOOH) on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> is the rate-limiting step for CO<sub>2</sub>-RR via pathway 3.

The over-potential for CO, HCOOH, HCHO, CH<sub>3</sub>OH and CH<sub>4</sub> production via Metal-based catalysts (Fe, Ni and Co single atom as catalysts, Cu, Au, Ag based bimetallic catalysts and Pt and Pd as metal catalysts) in previous works [11-15] are summarized in Table 4. The over-potential for CO, HCOOH, HCHO, CH<sub>3</sub>OH and CH<sub>4</sub> production on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages are reported in Table 4. The over-potential for CO, HCOOH, HCHO, CH<sub>3</sub>OH and CH<sub>4</sub> production on 2Cr-Si<sub>76</sub> nanocage is 0.30, 0.24, 0.27, 0.21 and 0.19 V. The over-potential for CH<sub>4</sub> and CH<sub>3</sub>OH formation are lower than HCOOH on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages. The over-potential for CO, HCOOH, HCHO, CH<sub>3</sub>OH and CH<sub>4</sub> production on 2Cr-C<sub>76</sub> nanocage is 0.36, 0.30, 0.33, 0.26 and 0.24 V. The over-potential for CO, CH<sub>4</sub>, HCOOH, HCHO and CH<sub>3</sub>OH on 2Cr-Si<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages are lower than 2Cr-C<sub>76</sub> nanocage. The over-potential of CO<sub>2</sub>-RR on 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> are lower than Fe, Ni and Co single atom as catalysts, Cu, Au, Ag based bimetallic catalysts and Pt and Pd as metal catalysts in previous works [11-15]. The over-potential for CO, HCOOH, HCHO, CH<sub>3</sub>OH and CH<sub>4</sub> production on 2Cr-B<sub>38</sub>N<sub>38</sub> nanocage is 0.34, 0.27, 0.31, 0.24 and 0.22 V. The 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> are catalyzed the CO<sub>2</sub>-RR to create the CO, CH<sub>4</sub>, HCOOH, HCHO and CH<sub>3</sub>OH with acceptable performance.

Table-4: The over-potential in V of CO<sub>2</sub>-RR on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages and reported over-potential in V of CO<sub>2</sub>-RR on Metal-based catalysts in previous works [11-15].

M06-2X			
Overpotential	2Cr-C <sub>76</sub>	2Cr-B <sub>38</sub> N <sub>38</sub>	2Cr-Si <sub>76</sub>
CO production	0.36	0.34	0.30
HCOOH production	0.30	0.27	0.24
HCHO production	0.33	0.31	0.27
CH <sub>3</sub> OH production	0.26	0.24	0.21
CH <sub>4</sub> production	0.24	0.22	0.19
PBEPBE			
Overpotential	2Cr-C <sub>76</sub>	2Cr-B <sub>38</sub> N <sub>38</sub>	2Cr-Si <sub>76</sub>
CO production	0.34	0.32	0.28
HCOOH production	0.28	0.25	0.22
HCHO production	0.31	0.29	0.25
CH <sub>3</sub> OH production	0.24	0.22	0.20
CH <sub>4</sub> production	0.22	0.21	0.18
B3LYP-D3			
Overpotential	2Cr-C <sub>76</sub>	2Cr-B <sub>38</sub> N <sub>38</sub>	2Cr-Si <sub>76</sub>
CO production	0.33	0.31	0.27
HCOOH production	0.27	0.25	0.22
HCHO production	0.30	0.28	0.25
CH <sub>3</sub> OH production	0.24	0.22	0.19
CH <sub>4</sub> production	0.22	0.20	0.17
Metal-based catalysts in previous works [11-15]			
Overpotential	Fe, Ni and Co single atom as catalysts	Cu, Au, Ag based bimetallic catalysts	Pt and Pd as metal catalysts
CO production	0.38	0.40	0.37
HCOOH production	0.31	0.34	0.30
HCHO production	0.35	0.37	0.34
CH <sub>3</sub> OH production	0.27	0.29	0.27
CH <sub>4</sub> production	0.25	0.27	0.25

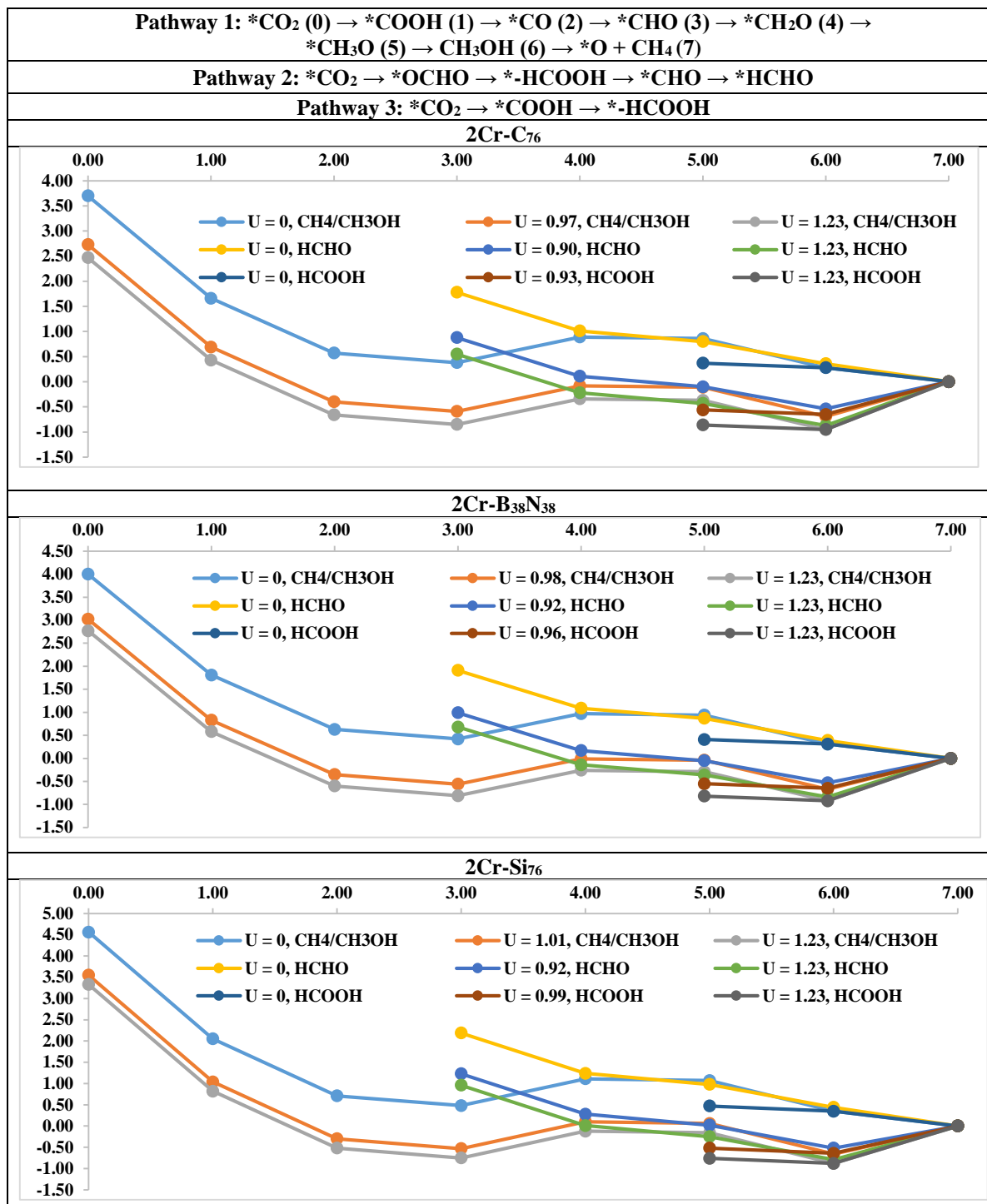


Fig. 4: The Gibbs free energy plan of reaction steps of CO<sub>2</sub>-RR on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages in various U values.

## Conclusion

The capacities of 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> as catalysts for CO<sub>2</sub>-RR to produce the CH<sub>4</sub> and CH<sub>3</sub>OH are investigated. The  $\Delta G_{\text{reaction}}$  of CO<sub>2</sub>-RR to

create CH<sub>4</sub> and CH<sub>3</sub>OH on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> are calculated. The limiting step of creation of CH<sub>4</sub> and CH<sub>3</sub>OH is \*CO → \*CHO on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub>. The over-potential for CO, HCOOH, HCHO, CH<sub>3</sub>OH and CH<sub>4</sub> production on

2Cr-B<sub>38</sub>N<sub>38</sub> nanocage is 0.34, 0.27, 0.31, 0.24 and 0.22 V. The over-potential of CO<sub>2</sub>-RR on 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> are lower than Fe, Ni and Co single atom as catalysts, Cu, Au, Ag based bimetallic catalysts and Pt and Pd as metal catalysts in previous works. The 2Cr-Si<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> nanocages has higher ΔG<sub>reaction</sub> and lower E<sub>barrier</sub> than 2Cr-C<sub>76</sub> for CO<sub>2</sub>-RR. The over-potential of creation of CH<sub>4</sub> and CH<sub>3</sub>OH on 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> are lower than HCOOH and HCHO. Finally, the 2Cr-Si<sub>76</sub>, 2Cr-C<sub>76</sub> and 2Cr-B<sub>38</sub>N<sub>38</sub> are suggested as catalysts for CO<sub>2</sub>-RR to create the CO, CH<sub>4</sub>, HCOOH, HCHO and CH<sub>3</sub>OH with high performance.

### Acknowledgment

I thank for my university for computational support.

### Ethical approval

All procedures performed in studies involving human participants were in accordance with the ethical standards of the institutional and/or national research committee and with the 1964 Helsinki declaration and its later amendments or comparable ethical standards.

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